## Comment on "Oscillations in the Bromomalonic Acid/Bromate System Catalyzed by $\left[\mathrm{Ru}(\mathrm{bipy})_{3}\right]^{2+}$ "

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In a recent study about the autocatalytic reaction between $\left[\mathrm{Ru}(\text { bipy })_{3}\right]^{2+}$ and bromate in 1 M sulfuric acid, a mechanism involving seven reactions, some of them reversible, was proposed to explain the time evolution of $\left[\mathrm{Ru}(\text { bipy })_{3}\right]^{2+}$ concentrations for different initial bromate concentrations. ${ }^{1}$ This reaction set is basically that proposed by Noyes, Field, and Thompsom ${ }^{2}$ (NFT) for the oxidation of cerium(III) by acidic bromate. The NFT mechanism can explain the bistability found in the $\mathrm{Ce}^{3+}-\mathrm{BrO}_{3}{ }^{-}$system and the bistability and oscillations found in a stirred flow reactor (CSTR) for the minimal bromate oscillator, $\mathrm{Ce}^{3+}-\mathrm{BrO}_{3}{ }^{-}-\mathrm{Br}^{-}$and $\mathrm{Mn}^{2+}-\mathrm{BrO}_{3}{ }^{-}-\mathrm{Br}^{-} .{ }^{3-10}$ The NFT set of reactions is the inorganic core of the mechanism proposed by Field, Körös, and Noyes ${ }^{11}$ (FKN) to explain the Belousov-Zhabotinsky (BZ) reaction. The NFT mechanism has been discussed, revised, and updated as a consequence of simulations and experimental results obtained from kinetics studies on specific reactions and from experimental work with oscillating systems related to the minimal bromate oscillator and to the BZ system. ${ }^{12-22}$

Starting with the minimal bromate oscillator catalyzed by [Ru(bipy) $]^{2+}$, exchanging the cerium by ruthenium complexes and keeping the numbering of the reactions according to ref 15 , we have the sequence

$$
\begin{gather*}
\mathrm{Br}^{-}+\mathrm{HOBr}+\mathrm{H}^{+} \rightleftarrows \mathrm{Br}_{2}+\mathrm{H}_{2} \mathrm{O}  \tag{R1}\\
\mathrm{Br}^{-}+\mathrm{HBrO}_{2}+\mathrm{H}^{+} \rightleftarrows 2 \mathrm{HOBr}  \tag{R2}\\
\mathrm{Br}^{-}+\mathrm{BrO}_{3}^{-}+2 \mathrm{H}^{+} \rightleftarrows \mathrm{HOBr}+\mathrm{HBrO}_{2}  \tag{R3}\\
\mathrm{HBrO}_{2}+\mathrm{H}^{+} \rightleftarrows \mathrm{H}_{2} \mathrm{BrO}_{2}^{+}  \tag{R4a}\\
\mathrm{HBrO}_{2}+\mathrm{H}_{2} \mathrm{BrO}_{2}^{+} \rightleftarrows \mathrm{HOBr}+\mathrm{BrO}_{3}^{-}+2 \mathrm{H}^{+}  \tag{R4b}\\
\mathrm{HBrO}_{2}+\mathrm{BrO}_{3}^{-}+\mathrm{H}^{+} \rightleftarrows \mathrm{Br}_{2} \mathrm{O}_{4}+\mathrm{H}_{2} \mathrm{O}  \tag{R5'}\\
\mathrm{Br}_{2} \mathrm{O}_{4} \rightleftarrows 2 \mathrm{BrO}_{2}^{-}
\end{gather*}
$$

$\left[\mathrm{Ru}(\text { bipy })_{3}\right]^{2+}+\mathrm{BrO}_{2} \cdot+\mathrm{H}^{+} \rightleftarrows\left[\mathrm{Ru}(\text { bipy })_{3}\right]^{3+}+\mathrm{HBrO}_{2}$

$$
\begin{equation*}
2 \mathrm{BrO}_{3}^{-}+2 \mathrm{H}^{+} \rightleftarrows \mathrm{HBrO}_{2}+\mathrm{HBrO}_{4} \tag{R6}
\end{equation*}
$$

What we want to point out is the inclusion of (R7) in this reaction set. Gao and Försterling ${ }^{1}$ included this reaction based on the instability of acidic bromate evidenced by $\mathrm{BrO}_{2}{ }^{-}$ formation in a 10 M sulfuric acid solution of bromate. ${ }^{23}$

Using $\Delta G_{\mathrm{f}}$ for $\mathrm{BrO}_{3}{ }^{-}, \mathrm{HBrO}_{2}$, and $\mathrm{HBrO}_{4}$ equal to $1.7,6.8$, and $122.09 \mathrm{~kJ} / \mathrm{mol}$, we calculate the equilibrium constant for (R7) as $1 \times 10^{-22.24,25}$ Ignoring the deviation from ideality, we calculate the equilibrium concentration for $\mathrm{HBrO}_{4}$ and

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Figure 1. Numerical integration results of the mechanism given by eqs R1-R7 (dashed lines) at initial $\left[\mathrm{BrO}_{3}{ }^{-}\right]$of (a) $1 \times 10^{-2} \mathrm{M}$, (b) 5 $\times 10^{-3} \mathrm{M}$, and (c) $3 \times 10^{-3} \mathrm{M}$ and initial concentration for $\mathrm{H}_{2} \mathrm{SO}_{4}$ and $\left[\mathrm{Ru}(\text { bipy })_{3}\right]^{2+}$ equal to 1 and $5.2 \times 10^{-5} \mathrm{M}$, respectively. Rate constants are the same as used by Gao and Försterling. ${ }^{1}$ Solid lines corresponds to (R7) turned off. Each solid line, from left to right, corresponds to background concentrations of $1 \times 10^{-8}, 1 \times 10^{-9}, 1 \times$ $10^{-10}, 1 \times 10^{-12}$, and, $1 \times 10^{-15} \mathrm{M}$, respectively. Results obtained with (R7) turned on for the background concentration $1 \times 10^{-8}, 1 \times$ $10^{-9}, 1 \times 10^{-10}, 1 \times 10^{-11}$, and $1 \times 10^{-15} \mathrm{M}$ are shown, from left to right, as dashed lines. There are five dashed lines too, but the first two $\left(1 \times 10^{-8}\right.$ and $\left.1 \times 10^{-9} \mathrm{M}\right)$ superimpose the solid lines calculated using these same background concentrations.
$\mathrm{HBrO}_{2}$ as equal to $2 \times 10^{-11} \mathrm{M}$ in a $10 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ and 0.2 M bromate solution (concentrations used in the Försterling and Murányi experiment ${ }^{23}$ ). At 1 M sulfuric acid and $3 \times 10^{-3} \mathrm{M}$ bromate concentrations, $\left[\mathrm{HBrO}_{4}\right]_{\mathrm{eq}}$ and $\left[\mathrm{HBrO}_{2}\right]_{\mathrm{eq}}$ are calculated as $3 \times 10^{-14} \mathrm{M}$. It means that, ignoring the activation energy barrier, equilibrium concentrations of the products of (R7) are in the range of trace amounts.

One piece of information that is usually omitted when reporting kinetics simulations are the initial concentration values used for species not present at the reaction beginning. It is a well-known fact that the algorithms used in the numerical integration of mechanistic models can produce a divide-by-zero condition when exact zero values are attributed to some concentration values. As a solution to this problem, it is usually to set an arbitrary "background" concentration in the range of $1 \times 10^{-10} \mathrm{M}$ for all the species not initially present.

Figure 1 shows the numerical integration results of the mechanism (R1)-(R7) (dashed lines) using the rate constants given by Gao and Försterling and starting at different background concentrations in the range from $1 \times 10^{-8}$ to $1 \times 10^{-15}$, for the three initial bromate concentrations given in Figure 3 of their paper. Results obtained turning off (R7) are presented as solid lines.

The numerical integrations were performed on a $486 / 33 \mathrm{MHz}$ PC-compatible microcomputer using a program written in Turbo Pascal to solve autonomous ordinary differential equation systems by a semiimplicit Runge-Kutta method. ${ }^{26}$

Our results show that background concentrations can affect the calculated concentration-time curves, depending on the mechanism considered. Comparing our Figure 1 with Figure 3 from the Gao and Försterling paper, we can estimate that the background concentration probably used by these authors was $1 \times 10^{-10} \mathrm{M}$.

As shown in Figure 1, (R1)-(R6) and (R1)-(R7) mechanisms produce quite the same results if background concentrations are equal to or greater than $1 \times 10^{-10} \mathrm{M}$. If background concentrations are lower than $1 \times 10^{-10}$, the results from each mechanism will differ greatly. In addition, mechanism (R1)(R7) will give the same concentration-time curves if background concentration is set lower than or equal to $1 \times 10^{-15}$ M.

Our conclusion is that one cannot say whether (R7) is occurring to produce the trace amounts of $\mathrm{HBrO}_{2}$ necessary to start the autocatalytic reaction between $\left[\mathrm{Ru}(\text { bipy })_{3}\right]^{2+}$ and acidic bromate. The agreement between simulation and experimental results using a background concentration of $1 \times 10^{-10} \mathrm{M}$ was
fortuitous. To increase the confidence on simulation results, one must specify the initials concentrations of impurities. Considering the influence of the $\mathrm{Br}^{-}$concentrations in (R1)(R3), this species appears to be one of the most important impurities to be evaluated in the reagents.

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